

# New Forms Of Contra-Continuity And Contra-Irresolute Maps In Nano Ideal Topological Spaces

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## ABSTRACT

The purpose of this paper is to present another class of functions referred to as contra  $nI_{gsemi}^*$  - continuous and contra  $nI_{gsemi}^*$ - irresolute functions in nano ideal topological space. Composition and decomposition of these functions under contra  $nI_{gsemi}^*$ -continuous and contra  $nI_{gsemi}^*$ - irresolute mappings are examined. Connections among these new classes and different classes of functions are laid out and few characterizations of these new classes of functions are studied.

Key words: contra  $nI_{gsemi}^*$  - continuous function, contra  $nI_{gsemi}^*$ - irresolute functions.

## I. Introduction:

Continuous and irresolute functions supply new way in the direction of research. In 1996, Dontchev [3] presented another class of functions called contra-continuous functions. Irresolute maps are introduced and studied by Crossley S.G and Hildebrand S.K [2] in 1972. Its significance is large in numerous regions of math and associated sciences. Parimala et al [10] presented the idea of nano ideal generalized closed sets in nano ideal topological spaces and researched a portion of its essential properties. As of late, Dr. J. Arul Jesti and J. Joycy Renuka [6] presented and concentrated on  $nI_{gsemi}^*$ -closed sets and  $nI_{gsemi}^*$ -open sets in nano ideal topological spaces. Pretty currently,

we [7] characterised  $nIgsemi^*$ -continuous and  $nIgsemi^*$ -irresolute functions in nano ideal topological spaces. In this paper, the conceptualization of  $nIgsemi^*$ -open sets and  $nIgsemi^*$ -continuous functions in nano ideal topological spaces are utilized to characterize and examine another class of maps referred to as contra  $nIgsemi^*$ -continuity and contra  $nIgsemi^*$ -irresolute functions in nano ideal topological spaces. Likewise, the characteristics and behaviours of contra  $nIgsemi^*$ -continuity and contra  $nIgsemi^*$ -irresolute functions in nano ideal topological spaces are mentioned.

## II. PRELIMINARIES

All through this paper  $(U, \tau_R(X))$  (or  $U$ ) address nano topological spaces on which no separation axioms are assumed except otherwise referred. For a subset  $A$  of a space  $(U, \tau_R(X))$ ,  $ncl(A)$  and  $nint(A)$  denote the nano closure of  $A$  and the nano interior of  $A$  respectively. We bear in mind the subsequent definitions, with the purpose to be utilized in the sequel.

**Definition 2.1** [6] A subset  $A$  of a nano ideal topological space  $(U, \mathcal{N}, I)$  is said to be **nano ideal generalized semi\*-closed** (briefly,  $nIgsemi^*$ -closed) if  $A_n^* \subseteq V$  whenever  $A \subseteq V$  and  $V$  is nano semi\*-open.

**Definition 2.2** [6] A subset  $A$  of a nano ideal topological space  $(U, \mathcal{N}, I)$  is said to be **nano ideal generalized semi\*-open** (briefly,  $nIgsemi^*$ -open) if  $X - A$  is  $nIgsemi^*$ -closed.

**Definition 2.3** [9,10] A subset  $A$  of a nano ideal topological space  $(U, \mathcal{N}, I)$  is  **$n^*$ -closed** if  $A_n^* \subseteq A$

**Definition 2.4** [5] A map  $f: (U, \mathcal{N}, I) \rightarrow (V, \mathcal{M}, J)$  is said to be  **$n^*$ -continuous** if  $f^{-1}(G)$  is  $n^*$ -closed in  $(U, \mathcal{N}, I)$  for every  $n$ -closed set  $G$  of  $(V, \mathcal{M}, J)$ .

**Definition 2.5** [12] A function defined between two nano topological spaces  $F: (U, \tau_R(S)) \rightarrow (U, \tau_R(T))$  is defined to be a  **$nIg$ -continuous function** if the the inverse image  $F^{-1}(P)$  is a  $nIg$ -open set in  $(U, \tau_R(S))$  for every  $n$ -open set  $P$  in  $(U, \tau_R(T))$ .

**Definition 2.6.** [1] A nano topological space  $(U, \tau_R(X))$  is said to be **nano-regular space**, if for each nano closed set  $F$  and each point  $x \in F$ , there exists disjoint nano open sets  $G$  and  $H$  such that  $x \in G$  and  $F \subset H$ .

**Remark 2.7** [5] 1. Every  $n$ -closed set is  $n^*$ -closed but not conversely .

2. Every  $n^*$ -closed set is  $nIg$ -closed but not conversely [9].

**Theorem 2.8.** [6] Consider a  $(U, \mathcal{N}, I)$ , then the implications are true and reverse implications are may not be true.

1. A nano closed is always a  $nI_{gsemi}^*$ -closed set.
2. A  $n^*$ -closed is always a  $nI_{gsemi}^*$ -closed set.
3. A  $ng$ -closed is always a  $nI_{gsemi}^*$ -closed set.
4. A  $nI_{gsemi}^*$ -closed is always a  $nI_g$ -closed set.
5. A nano open set is always a  $n^*$ -open set.

**Definition 2.9.** [7] A map  $f : (U, N, I) \rightarrow (V, M)$  is called  **$nI_{gsemi}^*$ -continuous function**, if  $f^{-1}(A)$  of each  $n$ -open set  $A \subseteq (V, M)$  is a  $nI_{gsemi}^*$ -open set in  $(U, N, I)$ .

**Definition 2.10.** [7] Consider two nano ideal topological spaces  $(U, N, I)$  and  $(V, M, J)$  and define a function  $f : (U, N, I) \rightarrow (V, M, J)$ . The function  $f$  is defined to be a  **$nI_{gsemi}^*$ -irresolute function**, if the inverse image  $f^{-1}(A)$  is a  $nI_{gsemi}^*$ -open set in  $(U, N, I)$  for every  $nI_{gsemi}^*$ -open set  $A$  in  $(V, M, J)$ .

### III. Contra $nI_{gsemi}^*$ - Continuous Functions

**Definition 3.1.** A function  $f : (U, N, I) \rightarrow (V, M, J)$  is referred to as contra  **$nI_{gsemi}^*$ - continuous** if  $f^{-1}(A)$  is a  $nI_{gsemi}^*$ -closed set of  $(U, N, I)$  for every  $n$ -open set  $A$  of  $(V, M)$ .

**Example 3.2.** Consider the universal set  $U = \{a, b, c, d\}$ , the approximation space  $U/R = \{\{a\}, \{c\}, \{b, d\}\}$ ,  $X = \{a, b\} \subseteq U$  and  $I = \{\varphi, \{a\}\}$ . The nano topology defined by  $U$  is  $\tau_R(X) = \{U, \varphi, \{a\}, \{b, d\}, \{a, b, d\}\}$  and  $nI_{gsemi}^*$ -closed sets are  $\{\{a\}, \{c\}, \{a, c\}, \{b, c\}, \{c, d\}, \{b, c, d\}, \{a, c, d\}, \{a, b, c\}, U, \varphi\}$ . Let  $V = \{a, b, c, d\}$ , the approximation space  $V/R = \{\{a\}, \{b\}, \{c, d\}\}$  and  $Y = \{b\}, \{d\} \subseteq V$ ,  $J = \{\varphi, \{a\}\}$ . The nano topology defined by  $V$  is  $\Omega_R(Y) = \{U, \varphi, \{b\}, \{c, d\}, \{b, c, d\}\}$  and  $nI_{gsemi}^*$ -closed sets are  $\{V, \varphi, \{b\}, \{c\}, \{d\}, \{c, d\}, \{b, d\}, \{b, c\}, \{b, c, d\}, \}$ . The function  $f : (U, N, I) \rightarrow (V, M, J)$  is defined as  $f(a) = b, f(b) = a, f(c) = c, f(d) = d$  is contra  $nI_{gsemi}^*$ -continuous function.

**Theorem 3.3.** Let  $f : (U, N, I) \rightarrow (V, M, J)$  be a function. Then the subsequent conditions are equal.

- (1)  $f$  is contra  $nI_{gsemi}^*$ -continuous.
- (2) If  $G$  is nano open set in  $V$ , then  $f^{-1}(G)$  is  $nI_{gsemi}^*$ -closed set in  $U$ .
- (3) If  $G$  is nano closed set in  $V$ , then  $f^{-1}(G)$  is  $nI_{gsemi}^*$ -open-set in  $U$ .
- (4) For each point  $u$  in  $U$  and every nano closed set  $G$  in  $V$  with  $f(u) \in G$ , there is an  $nI_{gsemi}^*$ -open set  $O$  in  $U$  containing  $u$  such that  $f(O) \subset G$ .

**Proof.** (1)  $\Rightarrow$  (2). Let  $G$  be nano open set in  $V$ . Then  $V - G$  is nano closed set in  $V$ . With the aid of meaning of contra nIgsemi\*-continuous function,  $f^{-1}(V - G)$  is nIgsemi\*-open set in  $U$ . However,  $f^{-1}(V - G) = U - f^{-1}(G)$ . This implies  $f^{-1}(G)$  is nIgsemi\*-closed set in  $U$ .

(2)  $\Rightarrow$ (3). The assumption of (2),  $f^{-1}(V - G)$  is nIgsemi\*-closed set in  $U$ . But  $f^{-1}(V - G) = U - f^{-1}(G)$ . This suggests,  $f^{-1}(G)$  is nIgsemi\*-open set in  $U$ .

(3)  $\Rightarrow$  (4). Let  $u \in U$  and  $G$  be any nano closed set in  $V$  with  $f(u) \in G$ . By means of (3),  $f^{-1}(G)$  is nIgsemi\*-open set in  $U$ . Let  $O = f^{-1}(G)$ . Then there is a nIgsemi\*-open set  $O$  in  $U$  containing  $u$  such that  $f(O) \subset G$ .

(4)  $\Rightarrow$  (1). Let  $u \in U$  and  $G$  be any n-closed set in  $V$  with  $f(u) \in G$ . Then  $V-G$  is n-open in  $V$  with  $f(u) \in G$ . By (4), there is a nIgsemi\*-open set  $O$  in  $U$  containing  $u$  such that  $f(O) \subset G$ . This means  $O = f^{-1}(G)$ . Hence,  $U - O = U - f^{-1}(G) = f^{-1}(V-G)$  which is nIgsemi\*-closed set in  $U$ .

**Proposition 3.4.** Every contra nIgsemi\*-continuous map is contra nIg-continuous.

**Proof.** Let  $f : (U, N, I) \rightarrow (V, M)$  be a contra nIgsemi\*-continuous map and let  $G$  be any nano open set in  $(V, M)$ . Then,  $f^{-1}(G)$  is nIgsemi\*-closed set in  $U$  Since every nIgsemi\*-closed set is nIg-closed,  $f^{-1}(G)$  is nIg-closed in  $U$ . Hence,  $f$  is contra nIg-continuous.

**Proposition 3.5.** In a nano topological space with an ideal  $I$ , If the function  $f : (U, N, I) \rightarrow (V, M, J)$  is contra nano generalised continuous function then  $f$  is nIgsemi\*-continuous function.

**Proof :** Let  $f : (U, N, I) \rightarrow (V, M)$  be a contra nano generalised continuous function. Let  $S$  be a nano open set in  $V$ . Since  $f$  is contra nano generalised continuous function,  $f^{-1}(S)$  is ng-closed in  $U$ . It is clear that every ng-closed set is nIgsemi\*-closed. In this manner,  $f^{-1}(S)$  is nIgsemi\*-closed in  $U$  which infers  $f$  is contra nIgsemi\* continuous function.

**Remark 3.6** Any contra nIgsemi\*-continuous function may not be a contra nano generalised continuous function. The subsequent illustration makes sense of this remark.

**Example 3.7.** Consider the universal set  $U = \{a, b, c, d\}$ , the approximation space  $U/R = \{\{a\}, \{c\}, \{b, d\}\}$ ,  $X = \{a, b\} \subseteq U$  with the ideal  $I = \{\emptyset, \{a\}\}$ . The nano topology defined by  $U$  is  $\tau_R(X) = \{U, \emptyset, \{a\}, \{b, d\}, \{a, b, d\}\}$  and nIgsemi\*-closed sets are

$\{U, \emptyset, \{a\}, \{c\}, \{a, c\}, \{b, c\}, \{c, d\}, \{b, c, d\}, \{a, c, d\}, \{a, b, c\}\}$ ,  
ng-closed sets are

$\{U, \varphi, \{c\}, \{b, c\}, \{c, d\}, \{a, c\}, \{b, d\}, \{a, b, c\}, \{b, c, d\}, \{a, c, d\}\}$   
 . Let  $V = \{a, b, c, d\}$ , the approximation space  $V/R = \{\{a\}, \{b\}, \{c, d\}\}$  and  $Y = \{\{b\}, \{d\}\} \subseteq V$  with the ideal  $J = \{\varphi, \{a\}\}$ . The nano topology defined by  $V$  is  $\Omega_R(Y) = \{U, \varphi, \{b\}, \{c, d\}, \{b, c, d\}\}$  and  $nIlgsemi^*$ -open sets are  $\{\{b\}, \{c\}, \{d\}, \{c, d\}, \{b, d\}, \{b, c\}, \{b, c, d\}, V, \varphi\}$ . The function  $f : (U, N, I) \rightarrow (V, M, J)$  is defined as  $f(a) = b, f(b) = a, f(c) = c, f(d) = d$  is a  $nIlgsemi^*$ -continuous function. Now  $f^{-1}(b) = \{a\}$  which is not  $ng$ -closed in  $U$ . Thus contra  $nIlgsemi^*$ -continuous function may not be a contra nano generalised continuous function.

**Theorem 3.8.** Let  $f : (U, N, I) \rightarrow (V, M, J)$  be a map and  $g : (U, N, I) \rightarrow ((U, N, I) \times (V, M, J))$  the graph map of  $f$ , defined by  $g(u) = (u, f(u))$  for every  $u \in U$ . If  $g$  is contra  $nIlgsemi^*$ -continuous, then  $f$  is contra  $nIlgsemi^*$ -continuous.

**Proof.** Let  $G$  be an nano open set in  $(V, M, J)$ . Then  $((U, N, I) \times G)$  is an nano open set in  $((U, N, I) \times (V, M, J))$ . It follows from theorem 3.3, that  $f^{-1}(G) = g^{-1}((U, N, I) \times G)$  is  $nIlgsemi^*$ -closed in  $(U, N, I)$ . Thus,  $f$  is contra  $nIlgsemi^*$ -continuous.

**Theorem 3.9.** If a map  $f : (U, N, I) \rightarrow (V, M, J)$  is contra  $nIlgsemi^*$ -continuous and  $V$  is nano regular, then  $f$  is  $nIlgsemi^*$ -continuous.

**Proof.** Let  $u$  be an arbitrary point of  $U$  and  $G$  be any  $n$ -open set of  $V$  containing  $f(u)$ . Given that  $V$  is nano regular, there exists an  $n$ -open set  $W$  in  $V$  containing  $f(u)$  such that  $A_n^*(W) \subset G$ . Since  $f$  is contra  $nIlgsemi^*$ -continuous, by theorem 3.3, there exists an  $nIlgsemi^*$ -open set  $O$  containing  $u$  such that  $f(O) \subset A_n^*(W)$ . Consequently,  $f(O) \subset A_n^*(W) \subset G$ . Thus  $f$  is  $nIlgsemi^*$ -continuous

**IV. Contra  $nIlgsemi^*$  - Irresolute Functions**

**Definition 4.1.** A function  $f : (U, N, I) \rightarrow (V, M, J)$  is called **contra  $nIlgsemi^*$  - irresolute** if  $f^{-1}(A)$  is a  $nIlgsemi^*$ -closed set of  $(U, N, I)$  for every  $nIlgsemi^*$ -open set  $A$  of  $(V, M, J)$ .

**Example 4.2.** Consider the universal set  $U = \{a, b, c, d\}$ , the approximation space  $U/R = \{\{a\}, \{d\}, \{b, c\}\}, X = \{a, d\} \subseteq U$  with the ideal  $I = \{\varphi, \{a\}\}$ . The nano topology defined by  $U$  is  $\tau_R(X) = \{U, \varphi, \{a, d\}\}$  and  $nIlgsemi^*$ -closed sets are  $\{U, \varphi, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}, \{c, d\}, \{b, d\}, \{b, c, d\}, \{a, c, d\}, \{a, b, d\}, \{a, b, c\}\}$   
 Let  $V = \{a, b, c, d\}$ , the approximation space  $V/R = \{\{a\}, \{b\}, \{c, d\}\}, Y = \{\{b\}, \{d\}\} \subseteq V$  with the ideal  $J = \{\varphi, \{a\}\}$ . The nano topology defined by  $V$  is  $\Omega_R(Y) =$

$\{V, \varphi, \{b\}, \{c, d\}, \{b, c, d\}\}$  and  $nIlgsemi^*$ -open sets are  $\{\{b\}, \{c\}, \{d\}, \{c, d\}, \{b, d\}, \{b, c\}, \{b, c, d\}, V, \varphi\}$ . The function  $f : (U, N, I) \rightarrow (V, M, J)$  is defined as  $f(a) = d, f(b) = b, f(c) = c, f(d) = a$  is a  $nIlgsemi^*$ -irresolute function.

**Theorem 4.3.** Let  $f : (U, N, I) \rightarrow (V, M, J)$  be a function. Then the following conditions are equivalent

- (1)  $f$  is contra  $nIlgsemi^*$ -irresolute.
- (2) If  $G$  is nano open set in  $V$ , then  $f^{-1}(G)$  is  $nIlgsemi^*$ -closed set in  $U$ .
- (3) If  $G$  is nano closed set in  $V$ , then  $f^{-1}(G)$  is  $nIlgsemi^*$ -open-set in  $U$ .
- (4) For each point  $u$  in  $U$  and each  $nIlgsemi^*$ -closed set  $G$  in  $V$  with  $f(u) \in G$ , there is an  $nIlgsemi^*$ -open set  $O$  in  $U$  containing  $u$  such that  $f(O) \subset G$ .

**Proof.** The proof is much like the theorem 3.3

#### V. Composition of Functions Under Contra $nIlgsemi^*$ -Continuous and Contra $nIlgsemi^*$ -Irresolute Functions.

**Theorem 5.1.** For the functions  $f : (U, N, I) \rightarrow (V, M, J)$  and  $g : (V, M, J) \rightarrow (W, O, K)$ ,  $g \circ f$  is  $nIlgsemi^*$ -irresolute, if  $f$  is contra  $nIlgsemi^*$ -irresolute map and  $g$  is contra  $nIlgsemi^*$ -irresolute map.

**Proof.** Let  $G$  be  $nIlgsemi^*$ -open set in  $W$ . Considering the fact  $g$  is contra  $nIlgsemi^*$ -irresolute,  $g^{-1}(G)$  is  $nIlgsemi^*$ -closed set in  $V$ . Since  $f$  is contra  $nIlgsemi^*$ -irresolute,  $(g \circ f)^{-1}(G) = f^{-1}(g^{-1}(G))$  is  $nIlgsemi^*$ -open set in  $U$ . Hence  $g \circ f$  is  $nIlgsemi^*$ -irresolute.

**Theorem 5.2.** For the functions  $f : (U, N, I) \rightarrow (V, M, J)$  and  $g : (V, M, J) \rightarrow (W, O, K)$ ,  $g \circ f$  is  $nIlgsemi^*$ -continuous, if  $f$  is contra  $nIlgsemi^*$ -continuous and  $g$  is contra nano continuous function.

**Proof:** Let  $f : (U, N, I) \rightarrow (V, M, J)$  be a contra  $nIlgsemi^*$ -continuous function and  $g : (V, M, J) \rightarrow (W, O, K)$  be a contra nano continuous function. Let  $S$  be a nano open set in  $W$ . Given that  $g$  is contra nano continuous function,  $g^{-1}(S)$  nano closed set in  $V$ . Since  $f$  is contra  $nIlgsemi^*$ -continuous function,  $f^{-1}(g^{-1}(S))$  is  $nIlgsemi^*$ -open in  $U$ . Hence  $g \circ f$  is  $nIlgsemi^*$ -continuous functions.

**Theorem 5.3** If the function  $f : (U, N, I) \rightarrow (V, M, J)$  is  $nIlgsemi^*$ -irresolute map and the function  $g : (V, M, J) \rightarrow (W, O, K)$  is contra  $nIlgsemi^*$ -continuous map, then  $g \circ f : (U, N, I) \rightarrow (W, O, K)$  is contra  $nIlgsemi^*$ -continuous map.

**Proof.** As  $g$  is contra  $nI_{gsemi}^*$ -continuous from  $(V, M, J)$  to  $(W, O)$ , for any nano open set in  $w$  as a subset of  $W$ , we obtain  $g^{-1}(w) = G$  is a  $nI_{gsemi}^*$ -closed set in  $(V, M, J)$ . Since  $f$  is  $nI_{gsemi}^*$ -irresolute map, we obtain  $(g \circ f)^{-1}(w) = f^{-1}(g^{-1}(w)) = f^{-1}(G) = S$  and  $S$  is a  $nI_{gsemi}^*$ -closed in  $(U, N, I)$ . Hence  $g \circ f$  is a contra  $nI_{gsemi}^*$ -continuous map.

**Theorem 5.4.** For the functions  $f : (U, N, I) \rightarrow (V, M, J)$  and  $g : (V, M, J) \rightarrow (W, O, K)$ ,  $g \circ f$  is contra  $nI_{gsemi}^*$ -continuous, if  $f$  is contra  $nI_{gsemi}^*$ -continuous and  $g$  is  $n$ -continuous functions.

**Proof:** Let  $S$  be a nano open set in  $W$ . Since  $g$  is  $n$ -continuous function,  $g^{-1}(S)$  is  $n$ -open set in  $V$ . Since  $f$  is contra  $nI_{gsemi}^*$ -continuous,  $f^{-1}(g^{-1}(S))$  is  $nI_{gsemi}^*$ -closed set in  $U$ . Then  $(g \circ f)^{-1}(S)$  is  $nI_{gsemi}^*$ -closed set in  $U$ . Hence  $g \circ f$  is contra  $nI_{gsemi}^*$ -continuous function.

**Remark 5.5.** The composition of two contra  $nI_{gsemi}^*$ -continuous function need not be contra  $nI_{gsemi}^*$ -continuous function and this is shown from the following example.

**Example 5.6** Let  $U = \{a, b, c, d\}$ , the approximation space  $U/R = \{\{a\}, \{b\}, \{c, d\}\}, X = \{c\} \subseteq U$  with the ideal  $I = \{\varphi, \{b\}, \{a, b\}\}$ . The nano topology defined by  $U$  is  $\tau_R(X) = \{U, \varphi, \{c, d\}\}$  and  $nI_{gsemi}^*$ -closed sets are

$U, \varphi, \{a\}, \{b\}, \{a, b\}, \{b, c\}, \{a, c\}, \{a, d\}, \{b, d\}, \{a, \{b\}\}, \{a, c, d\}$ .

Let  $V = \{a, b, c, d\}$ , the approximation space  $V/R = \{\{a\}, \{d\}, \{b, c\}\}, Y = \{a, d\} \subseteq V$  with the ideal  $J = \{\varphi, \{a\}\}$ . The nano topology defined by  $V$  is  $\Omega_R(Y) = \{V, \varphi, \{a, d\}\}$  and  $nI_{gsemi}^*$ -open sets are

$\{U, \varphi, \{a\}, \{b\}, \{c\}, \{c, d\}, \{a, b\}, \{b, d\}, \{b, c\}, \{a, c\}, \{a, b, c\}, \{a, b, d\}, \{a, c, d\}, \{b, c, d\}\}$ .

Let  $W = \{a, b, c, d\}$ , the approximation space  $W/R = \{\{b\}, \{d\}, \{a, c\}\}, Z = \{a, d\} \subseteq W$  with the ideal  $K = \{\varphi, \{d\}\}$ . The nano topology defined by  $W$  is  $\Psi_R(Z) = \{W, \varphi, \{d\}, \{a, c\}, \{a, c, d\}\}$  and  $nI_{gsemi}^*$ -closed sets are

$\{W, \varphi, \{b\}, \{d\}, \{b, d\}, \{b, c\}, \{a, b\}, \{b, c, d\}, \{a, b, d\}, \{a, b, c\}\}$

. Let the functions  $f$  and  $g$  can be defined as  $f :$

$U \rightarrow V$  defined by  $f(a) = a; f(b) = c; f(c) =$

$b; f(d) = d$  and  $g : V \rightarrow W$  is defined by  $g(a) =$

$d; g(b) = b; g(c) = c; g(d) = a$ . Here the functions  $f$

and  $g$  are contra  $nI_{gsemi}^*$ -continuous functions.

Since  $(g \circ f)^{-1}(\{a, c\}) = f^{-1}[g^{-1}(\{a, c\})] =$

$f^{-1}(\{c, d\}) = \{c, d\}$  and here  $\{c, d\}$  is not a  $nI_{gsemi}^*$ -

closed set in  $U$ ,  $g \circ f$  is not a  $nI g \text{semi}^*$ -continuous function.

**Theorem 5.7.** For the functions  $f : (U, N, I) \rightarrow (V, M, J)$  and  $g : (V, M, J) \rightarrow (W, O, K)$ , We have,

- (1)  $g \circ f$  is  $nI g \text{semi}^*$ -continuous, if  $f$  is contra  $nI g \text{semi}^*$ -continuous and  $g$  is contra  $n^*$ -continuous.
- (2)  $g \circ f$  is  $nI g \text{semi}^*$ -continuous, if  $f$  is contra  $nI g \text{semi}^*$ -irresolute and  $g$  is contra  $n^*$ -continuous.
- (3)  $g \circ f$  is  $nI g \text{semi}^*$ -continuous, if  $f$  is contra  $nI g \text{semi}^*$ -irresolute and  $g$  is contra  $nI g \text{semi}^*$ -continuous.
- (4)  $g \circ f$  is contra  $nI g \text{semi}^*$ -irresolute, if  $f$  is contra  $nI g \text{semi}^*$ -irresolute and  $g$  is  $nI g \text{semi}^*$ -irresolute.
- (5)  $g \circ f$  is contra  $nI g \text{semi}^*$ -irresolute, if  $f$  is  $nI g \text{semi}^*$ -irresolute and  $g$  is contra  $nI g \text{semi}^*$ -irresolute.

**Proof:** The proof of (1), (2), (3), (4) and (5) are much like theorem 5.1.

**Conclusion:** Through the above discussion we have summed up the conceptualization of contra  $nI g \text{semi}^*$ -continuity and contra  $nI g \text{semi}^*$ -irresolute functions in nano ideal topological spaces. Additionally, We laid out the connections between these new classes and different classes of functions with the use of appropriate illustrations.

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